

# Francesco Califano

Physics Department  
University of Pisa, Italy

*I plasmi nello spazio e in laboratorio:  
studio della dinamica di un sistema complesso*



**MASTER ITALO - FRANCESE  
DI FISICA INDIRIZZO PLASMI**

Un doppio diploma e un'esperienza internazionale  
Coordinato Pierre et Marie Curie  
Università di Pisa

L'UPMC e l'Università di Pisa cooperano per offrire un'opportunità unica d'integrazione, a livello di Master, nel contesto internazionale della ricerca di domani nell'ambito della fisica dei plasmi.

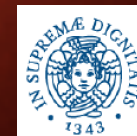
Questa formazione permette:

- di studiare per un anno in ciascuna delle due Università nell'ambito del Master Physics in Applications (UPMC) e della Laurea Magistrale in Fisica (UNIPD)
- di confrontarsi con due diverse culture accademiche
- di inserirsi nella rete di collaborazioni scientifiche Italo - francesi

**Importanti:**

- Possibilità di borsa di studio per il soggiorno nel paese di arrivo
- Selezione su dossier

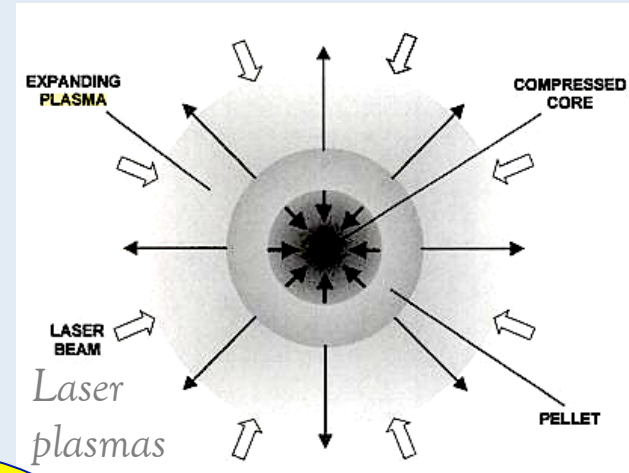
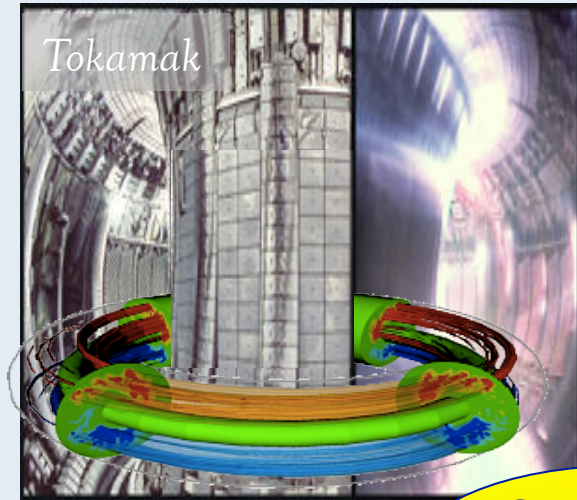
Per maggiori informazioni  
contattaci al link



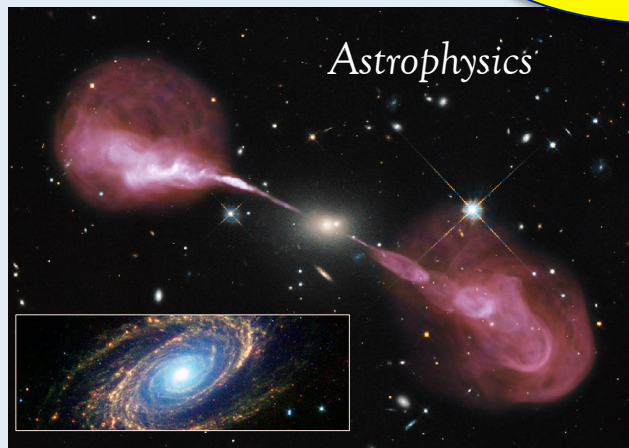
For many observed phenomenon *very similar physical mechanism*

**Plasmas are produced in the laboratory mainly for fusion purpose**

toroidal'naya kamera s magnitnymi katushkami  
toroidal chamber with magnetic coils



Complex and  
fascinating systems





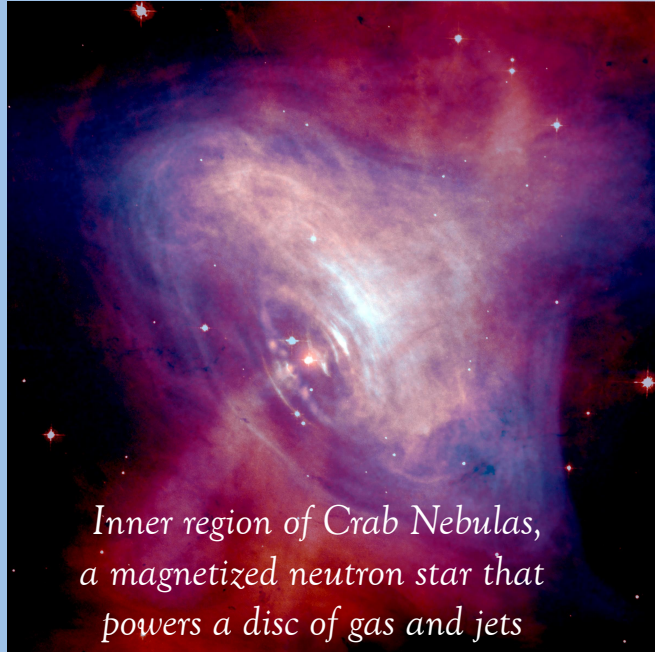
*Astrophysics, very spectacular objects:  
accretion disk, stars, black-holes, jets, ...*



*Elliptical galaxy emitting  
a relativistic jet [ M87 ]*



*Lagoon Nebula: a giant interstellar  
cloud in the constellation Sagittarius*



*Inner region of Crab Nebulas,  
a magnetized neutron star that  
powers a disc of gas and jets*

*Plasmas: hot and/or rarefied  
systems almost collisionless*



# *Why space plasmas are so important for plasma physics ?*

Significant technical developments in space observations have offered the possibility to obtain *measurements of electric and magnetic fields*, density, etc...with a sufficient resolution (in space and time) to reach the *kinetic scales*, such as the Debye length and electron plasma frequency.

It is today possible to *investigate the fine structuring of space plasmas* and its role in converting the large-scale macroscopic motions in thermal energy, in particle acceleration as well as in the heat transport that drive the dynamics and/or the stability of space plasmas.

*Space plasmas: a laboratory of excellence  
for collisionless plasma dynamics*



# Aurora: a beautiful phenomenon arising by the intrinsic coupling of the Earth – Magnetosphere – Sun system

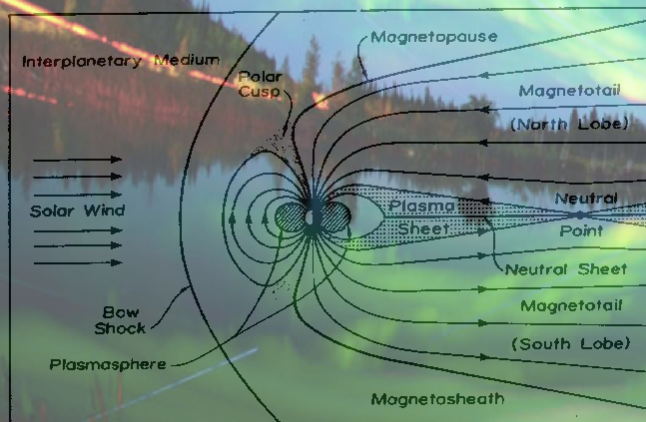
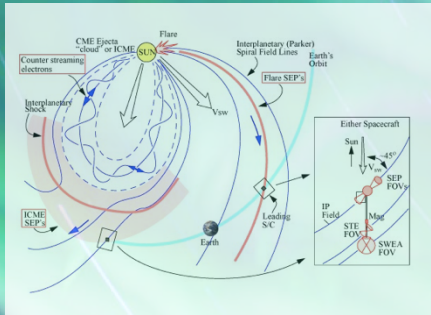
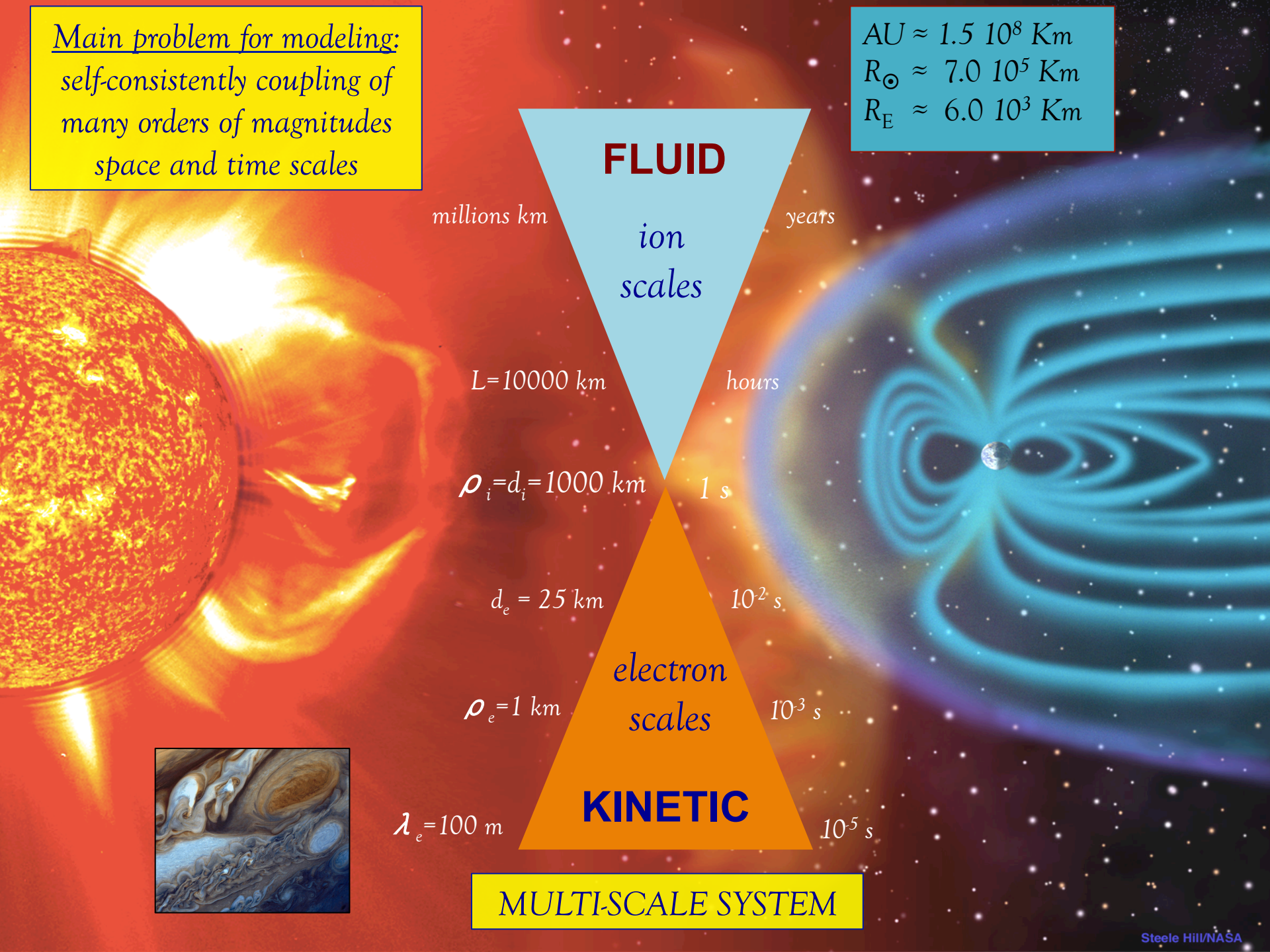


Figure 1



Main problem for modeling:  
self-consistently coupling of  
many orders of magnitudes  
space and time scales

$$\begin{aligned} \text{AU} &\approx 1.5 \cdot 10^8 \text{ Km} \\ R_{\odot} &\approx 7.0 \cdot 10^5 \text{ Km} \\ R_{\text{E}} &\approx 6.0 \cdot 10^3 \text{ Km} \end{aligned}$$



MULTI-SCALE SYSTEM



*How may we study  
such a complex system ?*

*A plasma is a collection  
of discrete charged particles  
globally neutral behaving as a  
collective system dominated by  
long-range electromagnetic forces*

*Main problem for theory: such systems are not in  
equilibrium because collisions are very rare*

*Plasmas are the realm of long range collective interactions: binary interactions  
("collisions") play a secondary, in some conditions even a negligible, role*



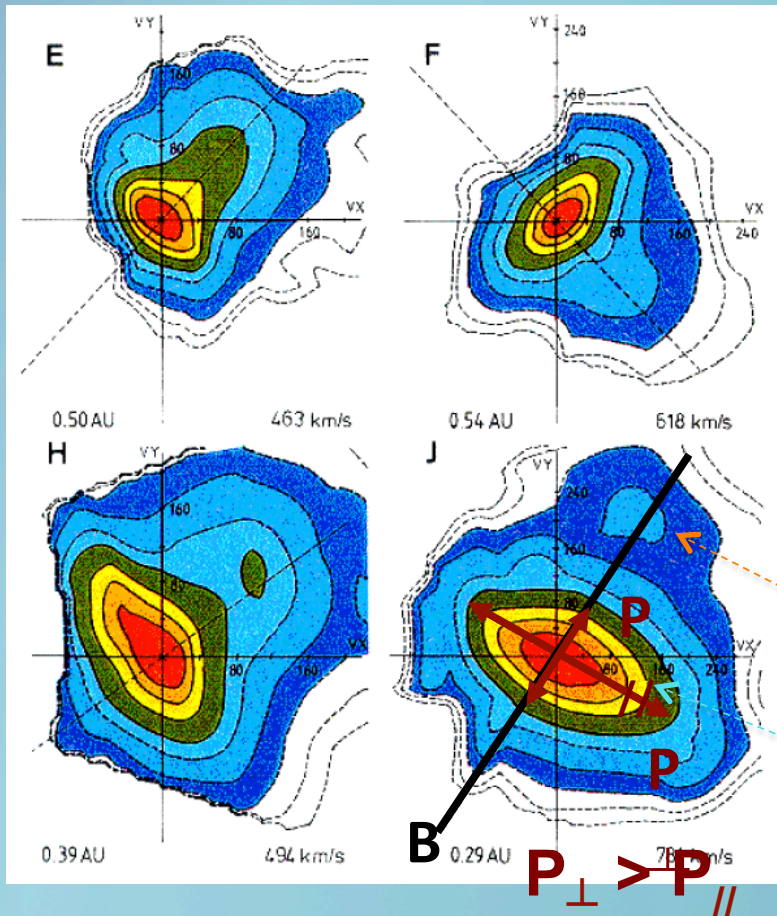
# Lack of collisions observed in space

Proton velocity distribution functions in *velocity space*, as measured by Helios in the fast solar wind.

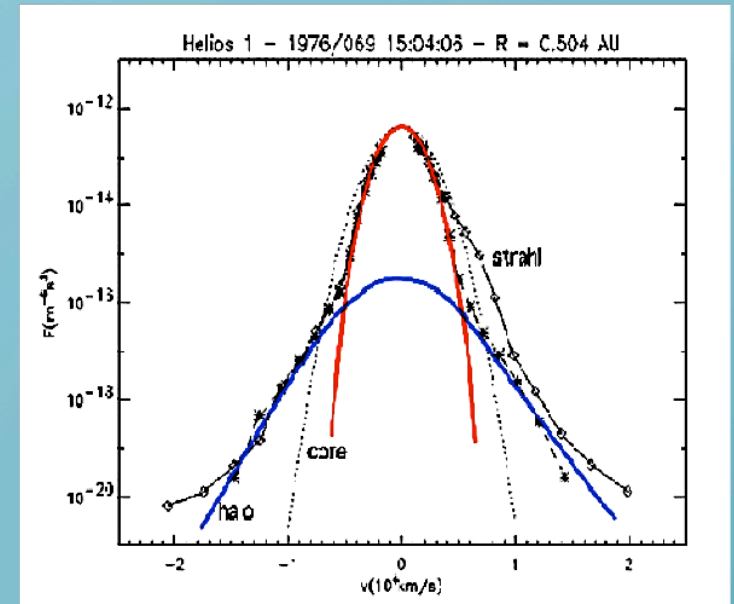
Neutral Gaz:  $\nu_{\text{coll}} \gg \omega$

Plasma:  $\omega \gg \nu_{\text{coll}}$

Problems for plasma  
thermodynamics!



Non-Maxwellian Distribution function  
routinely observed in the solar wind



particle beam  
pressure anisotropy



*We can see our plasma as a almost collisionless  
long range interactions MANY BODY SYSTEM*

*Plasmas are the realm of long range collective interactions: binary interactions ("collisions") play a secondary, in some conditions even a negligible, role*

*Too many particles for a N-body  
description even for the last  
generation of super-computers*

**WE NEED A  
CONTINUOUS  
DESCRIPTION!**





The idea is to use statistical description of a  $N$  particles system based on the probability densities  $F$  giving the probability of finding simultaneously the particles at locations  $(x_1, x_2, \dots, x_N)$  in phase space.

By assuming the particle kinetic energy is much larger than the typical potential energy due to its nearest neighbor,  $E_k \ll \Phi$ , we can simplify by using the reduced probability function  $f_s(x_1, \dots, x_s, v_1, \dots, v_s)$  by integrating the d.f. allover the particles except 1 to  $s$ :

$$f_s(x_1, \dots, x_s, v_1, \dots, v_s) = \int F_n(x_1, \dots, x_n, v_1, \dots, v_n) dx_{s+1}, \dots, x_n, v_{s+1}, \dots, v_n,$$

The probability density contains the effects of the interactions among particles. Each particle interacts at first with the whole system while we neglect interactions with nearby particles

We need to reduce  $s$  as small as possible, i.e. to have particles  
“quasi non-correlated”



When the interaction potential among particles is “small”, the probability densities can be written through a cluster expansion:

Inter-particle forces can be divided into:

1. *mean force* (“many” distant particles)
2. Force due to nearest neighbor particles

*Forces that do not depend on the exact location of all particles have the appearance of external forces.*

$$F_2(\mathbf{x}_1, \mathbf{x}_2) = F_1(\mathbf{x}_1) F_1(\mathbf{x}_2) [1 + \cancel{P_{12}(\mathbf{x}_1, \mathbf{x}_2)} + \cancel{\dots}]$$

$P_{12}$ : two particle correlation function

*In general, single particle interactions are assumed as negligible*

EACH PARTICLE INTERACTS WITH THE FULL SYSTEM

IN OTHER WORDS THE DISTRIBUTION FUNCTION EVOLVES UNDER THE ACTION OF THE E.M. FIELDS GENERATED BY ALL PARTICLES



***IN CONCLUSION, Plasma collisionless dynamics is described by  
The Vlasov equation for the  $f^1(x,v,t)$  (3D-3V phase space)***

*(neglecting collisions)*

$$\frac{\partial f_a}{\partial t} + \underline{v} \cdot \frac{\partial f_a}{\partial \underline{x}} + \frac{q_a}{m} \left( \underline{E} + \frac{\underline{v} \times \underline{B}}{c} \right) \cdot \frac{\partial f_a}{\partial \underline{v}} = 0$$

*Liouville equation in phase space*

*Here  $f_a$  is the **distribution function** of  $a$ -species,  $\underline{E}$  and  $\underline{B}$   
the electromagnetic fields self-consistently generated by the whole system*

*The **Vlasov equation**, self-consistently coupled to the Maxwell  
equations is the **basic model for a collisionless plasma***



# FROM VLASOV TO FLUID

Macroscopic equations and variables are obtained as velocity moments of the d.f.;

*why? because it is very difficult to solve the Vlasov equation*

$$\int \mathbf{v}^n \left[ \frac{\partial f_a}{\partial t} + \mathbf{v} \cdot \frac{\partial f_a}{\partial \mathbf{x}} + \frac{q_a}{m} \left( \mathbf{E} + \frac{\mathbf{v} \times \mathbf{B}}{c} \right) \cdot \frac{\partial f_a}{\partial \mathbf{v}} \right] d\mathbf{v} = 0$$

Continuity (n=0), Momentum (n=1), and so on equations are obtained by integrating the  $\mathbf{v}^n$  moment of the Vlasov equation.

Number of particles, m=0

$$n_a(\mathbf{x}, t) = \int f_a(\mathbf{x}, \mathbf{v}, t) d\mathbf{v}$$

Current density, m=1

$$J_a(\mathbf{x}, t) = q_a n_a \mathbf{V}_a(\mathbf{x}, t) = q_a \int \mathbf{v} f_a(\mathbf{x}, \mathbf{v}, t) d\mathbf{v}$$

Pressure tensor,  
scalar pressure

$$P_a(\mathbf{x}, t) = m_a \int \mathbf{w}_a \mathbf{w}_a f_a(\mathbf{x}, \mathbf{v}, t) d\mathbf{v} \quad \mathbf{w}_a = \mathbf{v} - \mathbf{V}_a$$

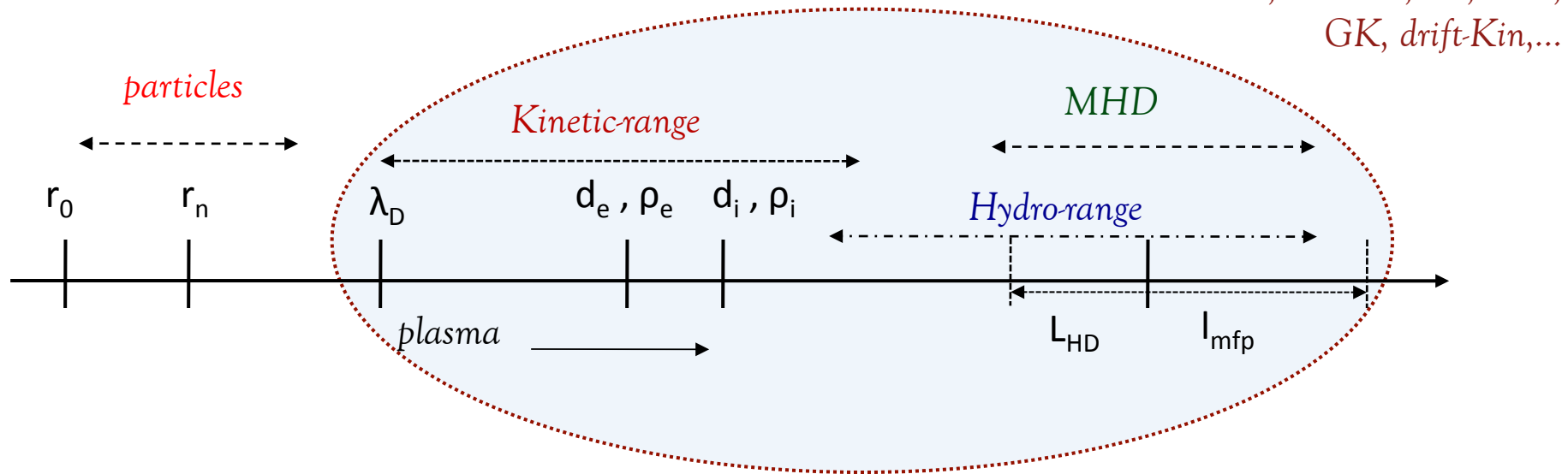
heat flux, ....

$$\mathbf{q}_a(\mathbf{x}, t) = \frac{1}{2} m_a n_a \int |\mathbf{w}_a|^2 \mathbf{w}_a f_a(\mathbf{x}, \mathbf{v}, t) d\mathbf{v}$$

***Even if a plasma is not a fluid !***

*.....closure problems.....*

*A plasma is a multi-scale (multi-frequency) system. Most of the models focus on a regime corresponding to a particular range of scales*



$$r_0 = e^2 / T$$

[ distance of min. approach (  $E_k \sim \Phi_C$  ) ]

$$r_n = n^{-1/3}$$

[ mean particle distance ]

$$\lambda_D = \sqrt{T / 4\pi n e^2}$$

[ Debye length ]

$$d_{e/i} = c / \omega_{e/i}$$

[ e/i inertial length ,  $\omega_e$  = plasma freq. ]

$$\rho_{e/i} = v_{th,e/i} / \Omega_{ce,ci}$$

[ e/i Larmor radius,  $\Omega_{ce,ci}$  = cycl. freq. ]

$$L_{HD} (>> \lambda_D, \rho_{e/i})$$

[ hydro scale ]

$$l_{mfp}$$

[ mean free path ]

$$\bullet \quad L \geq \lambda_D$$

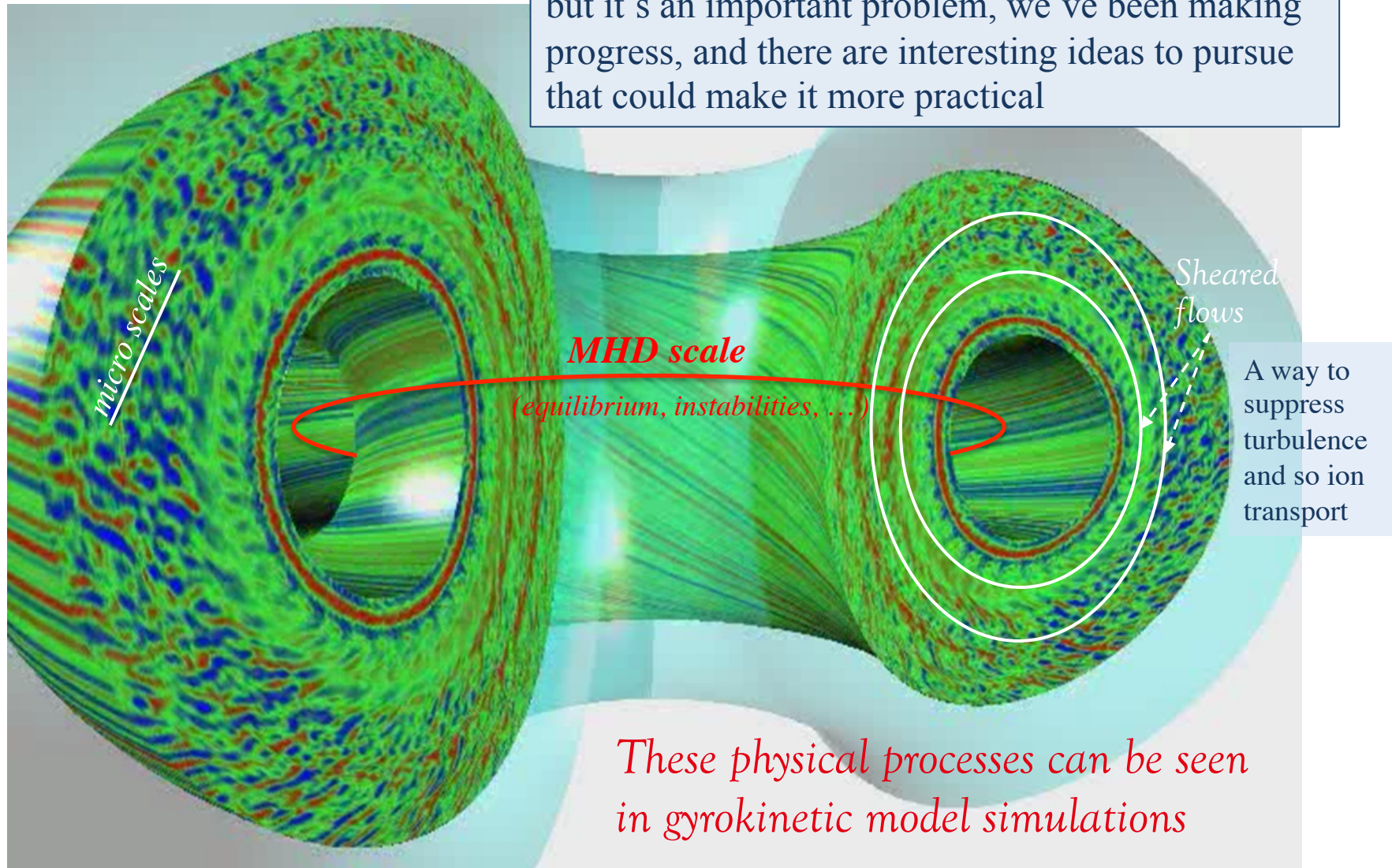
*A plasma must be “larger”  
than the Debye length  
(screening distance)*



# Turbulence, one of most important processes in plasmas, one of the best example of multi-scale physics

Here turbulence play a key role in transport

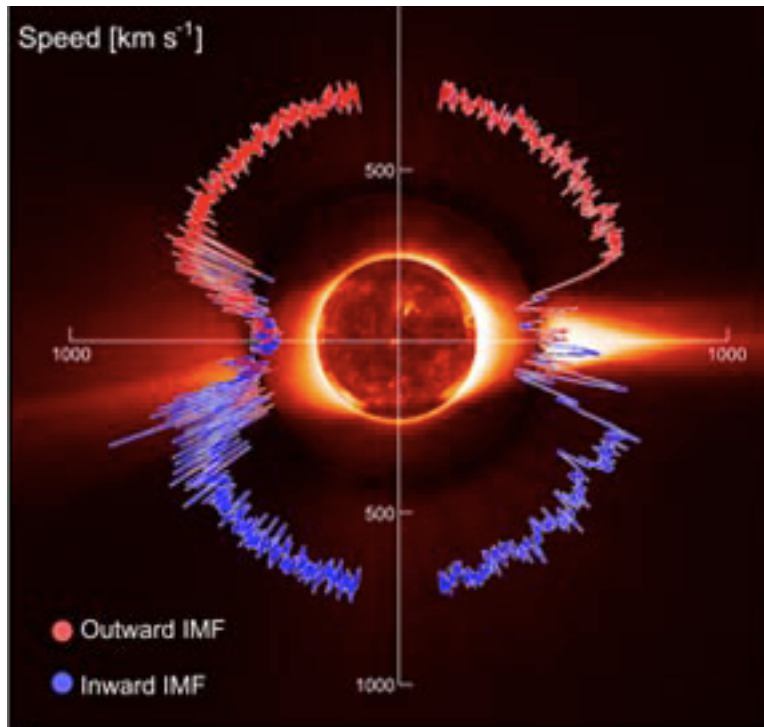
Fusion energy is hard and it will take a lot of time, but it's an important problem, we've been making progress, and there are interesting ideas to pursue that could make it more practical



These physical processes can be seen  
in gyrokinetic model simulations

# Heating in space

*The interplanetary plasma generated by the Sun and filling the Heliosphere, is known to be hotter than expected in an expanding plasma.*



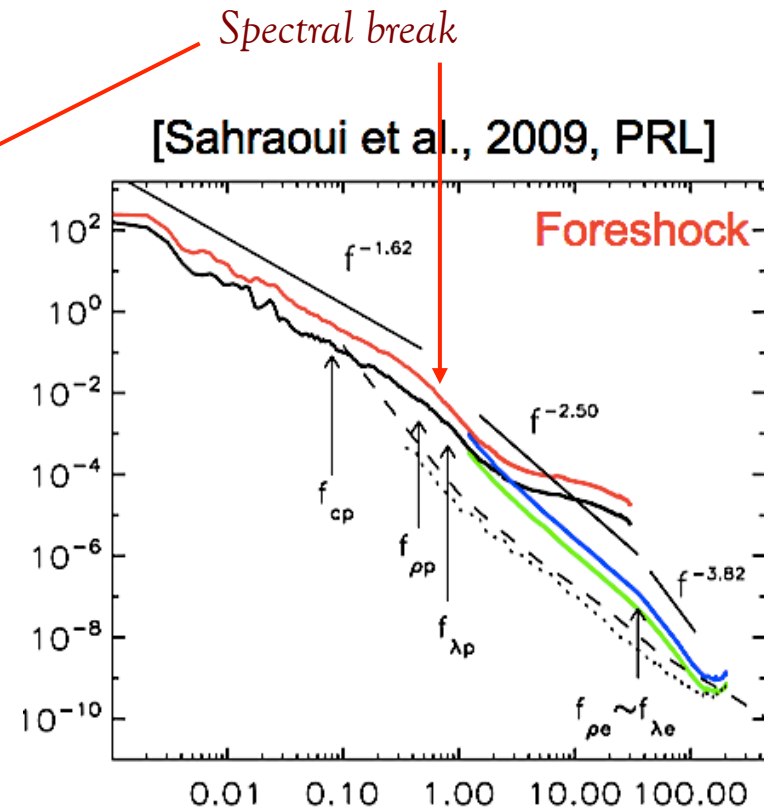
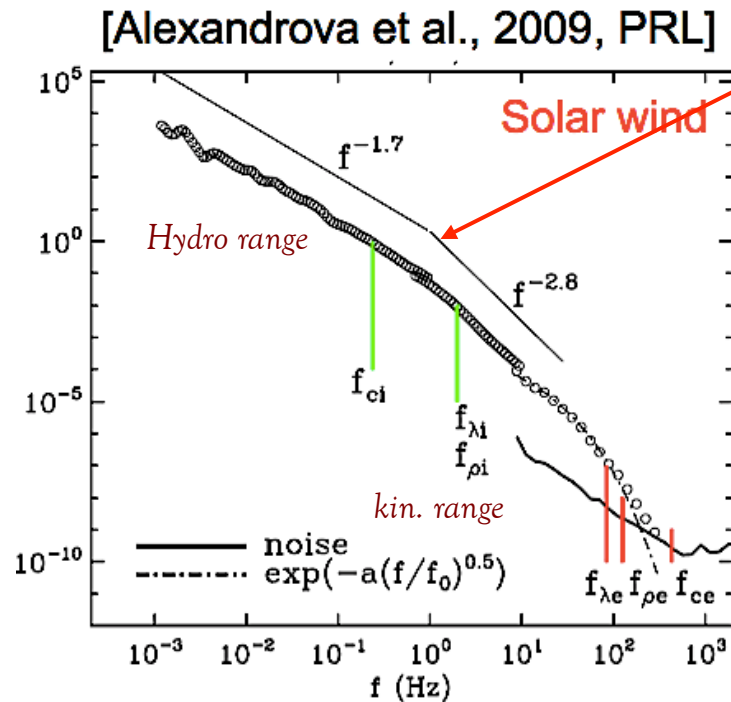
## Solar Wind

Understanding *how energy* from the Sun *can be* “*dissipated*” into heat in such a collision-free system represents a top priority in space physics.

*Here turbulence again play a key role*



# Turbulence at electron scales: Cluster observations

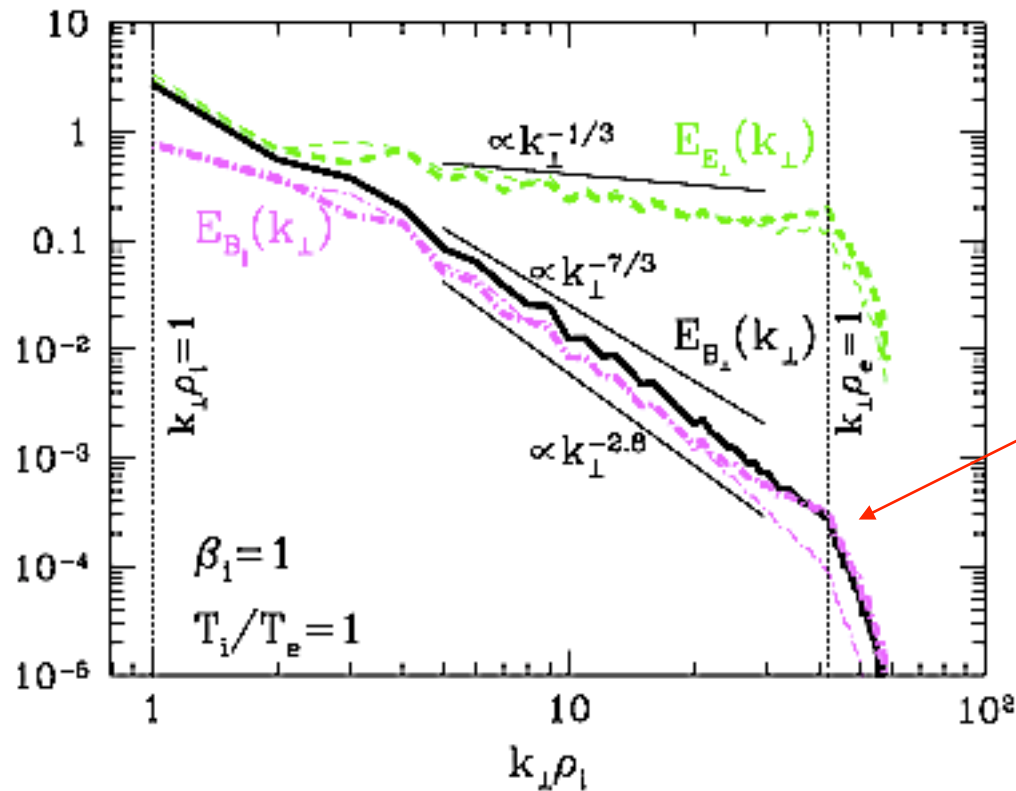


In the solar wind the energy cascade is supported primarily by Alfvén waves or Alfvénic fluctuations at MHD scales and by kinetic Alfvén waves (KAWs) at kinetic scales  $k_{\perp} \rho_i \geq 1$ .

# Gyro-kinetic simulation of solar wind turbulence with correct mass ratio

(model developed in the laboratory context)

Howes et al., PRL, 2011



Kinetic Alfvén waves cascade can produce a nearly power-law behavior over the dissipation range.

Dissipation is due to resolved collisionless damping via Landau resonances.

Thick lines: perpendicular and parallel magnetic (solid, dot-dashed), electric (dashed) energy spectra.  
Thin lines: perpendicular electric (dashed) and parallel magnetic (dot-dashed) energy spectra of the KAW model.

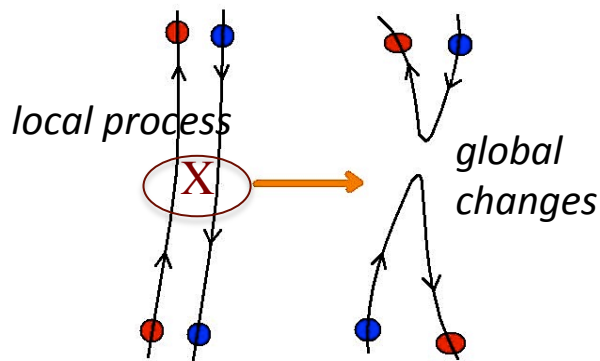


# Magnetic Reconnection is also a multi-scale process

one of the most important processes in plasmas

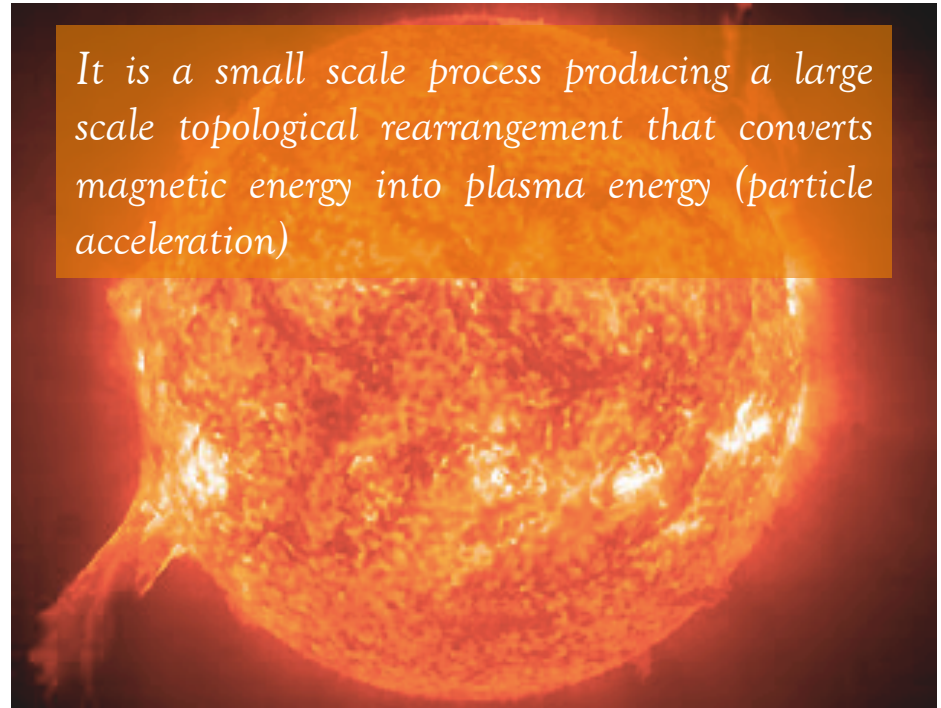
It affects the *global energy balance of the system* (astrophysics)

reorganizes the *large scale magnetic topology* (laboratory)



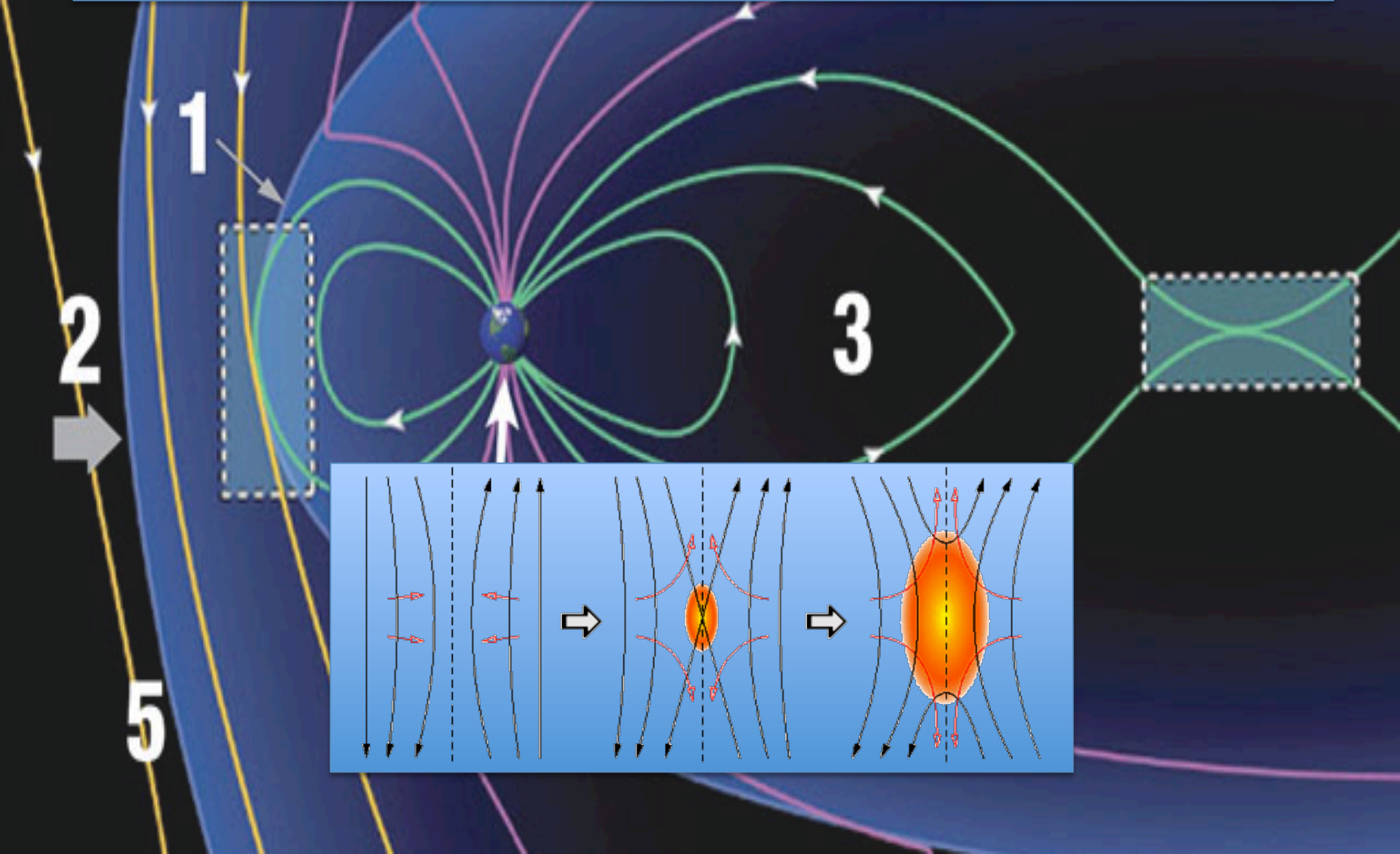
Release of the magnetic energy confined in the plasma can occur if the large-scale topological constraints get broken

It is a small scale process producing a large scale topological rearrangement that converts magnetic energy into plasma energy (particle acceleration)



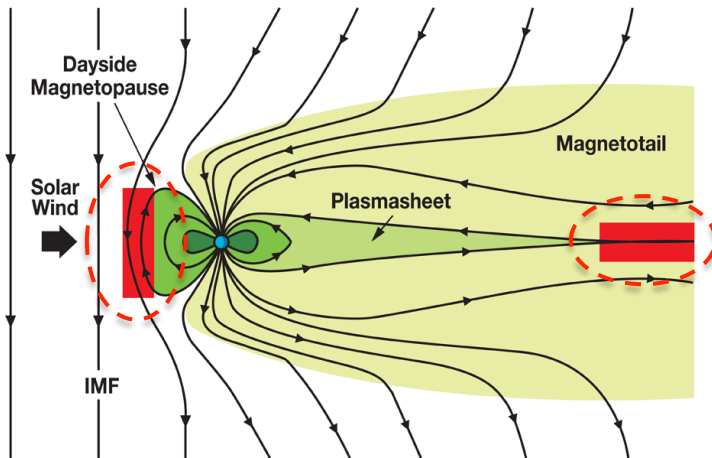
*Very strong and rapid energy release observed in space and laboratory*

**Magnetic reconnection** is a physical process in highly conducting plasmas in which the magnetic topology is rearranged and magnetic energy is converted to kinetic energy, thermal energy, and particle acceleration.

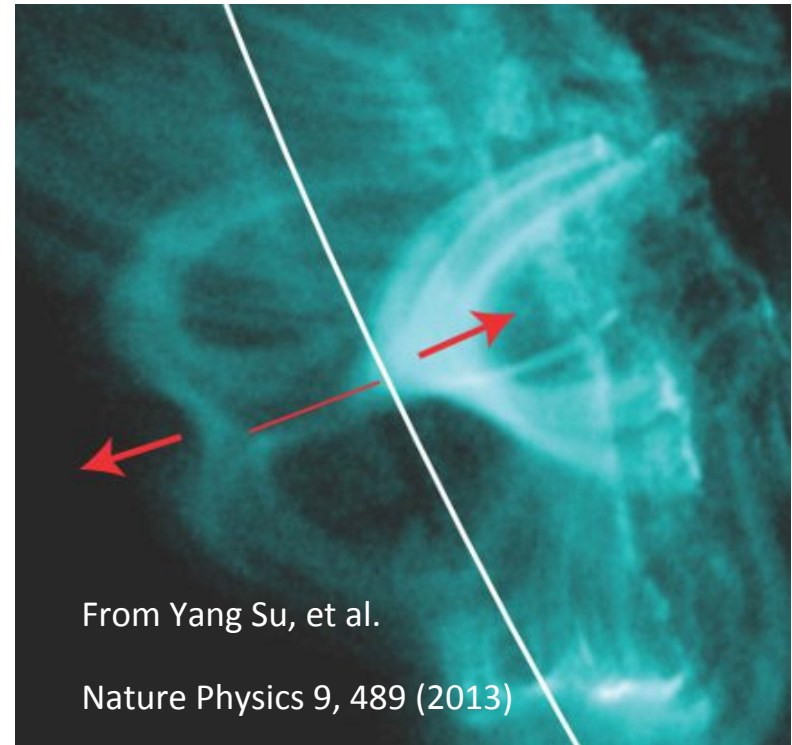




# Reconnection in space



*magnetic reconnection is responsible for solar wind plasma transfer into the magnetosphere, magnetic sub-storms, acceleration of beam particles, ...*



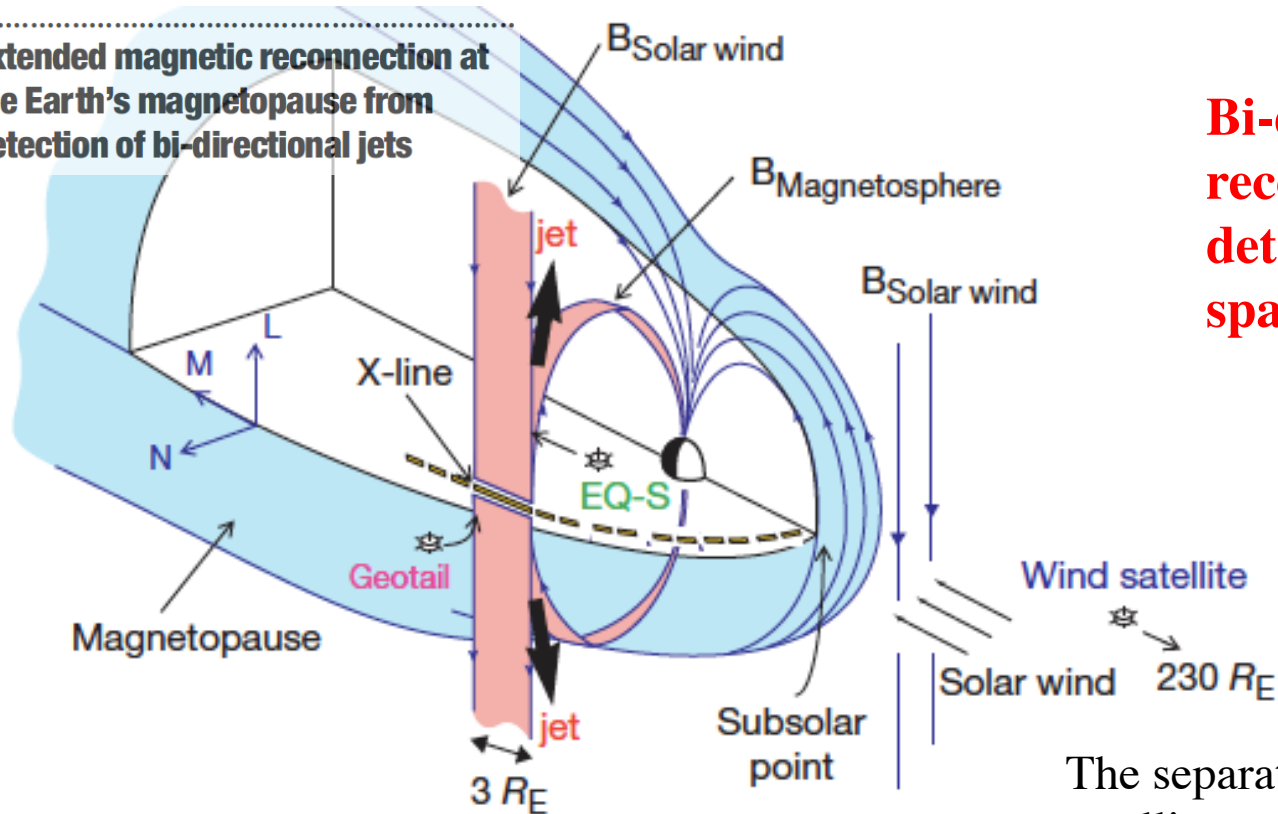
“The flare, which occurred on 17 August 2011 lasted about 20 minutes. It was ideally positioned at the edge of the visible solar disk (white curve). Loops of hot plasma pinned to magnetic field lines were seen to move from opposite sides toward the red line, reconnect, and flow outward in the directions of the red arrows.

Reconnection is believed to be the dominant process by which solar-wind energy enters the Earth's magnetosphere

This energy is subsequently dissipated by magnetic storms and aurorae

#### letters to nature

Extended magnetic reconnection at the Earth's magnetopause from detection of bi-directional jets



Three-dimensional cutaway view of the magnetosphere showing the spacecraft positions and the presence of an extended reconnection line.

The separation between the Geotail satellite and the Equator satellite was  $4 R_E$  in the north-south And  $3 R_E$  in the east-west direction.



# Reconnection in laboratory

Plasma Phys. Control. Fusion **53** (2011) 013001

Topical Review

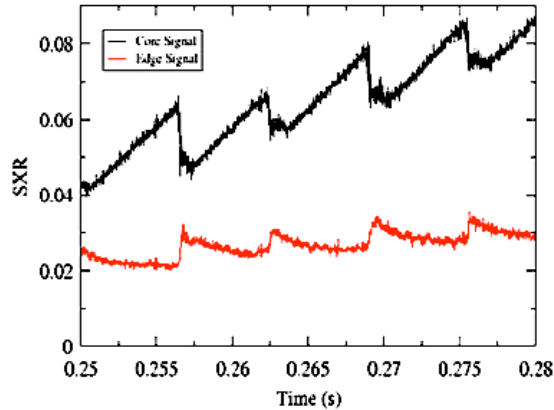
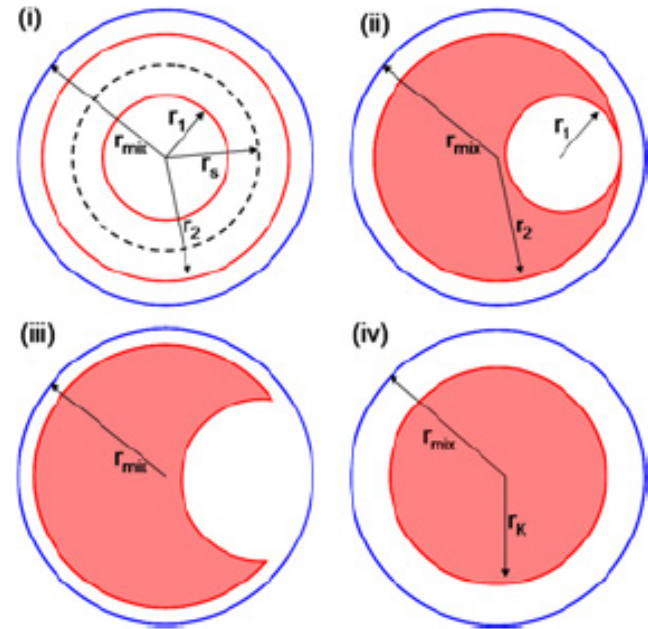


Figure 2. The measured soft x-ray signal during MAST discharge 8360. At each sawtooth crash the central soft x-ray emission exhibits a rapid decrease, whilst concurrently the edge plasma shows an increase in emission.

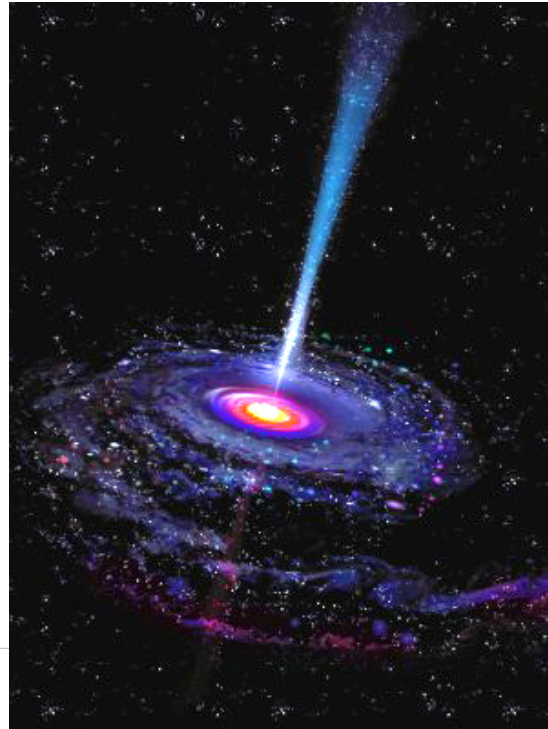
Magnetic and thermal energy release in a series of reconnection events in a toroidal fusion plasma. The change of magnetic topology makes a “punch” in the magnetic confinement. This allows the hotter central part of the plasma to escape towards the plasma boundaries.



A poloidal cross section of the plasma torus is shown at successive times. The magnetic field lines of the un-reconnected configuration follow helices that wind up on nested toroidal surfaces. The circles in frame i) are poloidal sections of such surfaces

# Reconnection in Astrophysics

An accretion disc is a structure formed by diffuse material in orbital motion around a massive central body (typically a star). Gravity causes material in the disc to spiral inward towards the central body



Dynamo theory, *based on small scale reconnection*, describes the process through which a rotating, convecting, and electrically conducting fluid can maintain a magnetic field over astronomical time scales



THE ASTROPHYSICAL JOURNAL, 773:118 (16pp), 2013 August 20  
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637X/77

## PARTICLE ACCELERATION DURING MAGNETOROTATIONAL INSTABILITY IN A COLLISIONLESS ACCRETION DISK

MASAHITO HOSHINO

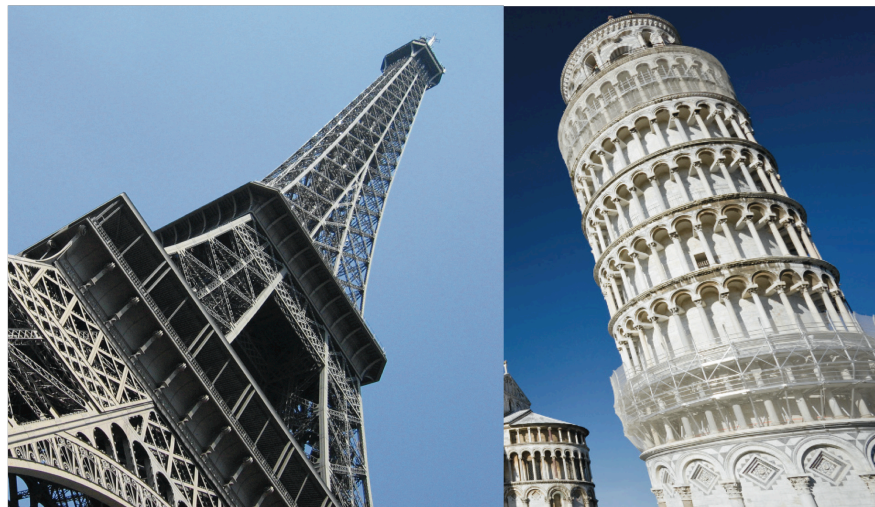
Department of Earth and Planetary Science, The University of Tokyo, Tokyo 113-0033, Japan; [hoshino@eps.s.u-tokyo.ac.jp](mailto:hoshino@eps.s.u-tokyo.ac.jp)

Received 2013 May 16; accepted 2013 June 25; published 2013 August 1

### ABSTRACT

Particle acceleration during the magnetorotational instability (MRI) in a collisionless accretion disk was investigated by using a particle-in-cell simulation. We discuss the important role that magnetic reconnection plays not only on the saturation of MRI but also on the relativistic particle generation. The plasma pressure anisotropy of  $p_{\perp} > p_{\parallel}$  induced by the action of MRI dynamo leads to rapid growth in magnetic reconnection, resulting in the fast generation of nonthermal particles with a hard power-law spectrum. This efficient particle acceleration mechanism involved in a collisionless accretion disk may be a possible model to explain the origin of high-energy particles observed around massive black holes.





# MASTER ITALO - FRANCESE DI FISICA INDIRIZZO PLASMI

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Università di Pisa

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- > di inserirsi nella rete di collaborazioni scientifiche italo - francesi

### Importante!

- Possibilità di borse di studio per il soggiorno nel paese straniero
- Selezione su dossier

Per maggiori informazioni  
[califano@df.unipi.it](mailto:califano@df.unipi.it)





*“Master de Physique  
Fondamentale et  
Applications”*

*“Laurea  
Magistrale  
in Fisica”*

**Dual Master Diploma  
University Pierre and Marie  
Curie University of Pisa**

*The Partner Universities agree to start a joint  
programme aimed at awarding a **Dual Degree***



# Dual Master Diploma Students of the University of Pisa

## First year in Pisa (fundamental courses)

| CURRICULUM Structure of Matter - Plasmas, M2 at UPMC (Paris) Pisa students                   |                                   |        |      |            |
|--|-----------------------------------|--------|------|------------|
| ITALIAN STUDENT First year (PISA) 60 ECTS. At least 51 before departure (60 before February) |                                   |        |      |            |
| Numero   | Denominazione                     | SSD    | ECTS | CFU TOTALI |
| <b>COURSES (mandatory)</b>   |                                   |        |      |            |
| 1  | Struttura della Materia 2         | FIS 03 | 9    | 9          |
| 1  | Laboratorio di Ottica Quantistica | FIS 01 | 12   | 12         |
| 1 at choice  | Fisica Teorica 1                  | FIS 02 | 9    | 9          |
|  | Fisica Statistica                 | FIS 02 | 9    |            |
| 1 at choice  | Fisica dello Stato Solido         | FIS 03 | 9    | 9          |
|  | Fluidodinamica                    | FIS 03 | 9    |            |
| 4  | <b>TOTAL ECTS</b>                 |        |      | <b>39</b>  |
| <b>COURSES at choice</b>   |                                   |        |      |            |
|  | <b>TOTAL ECTS</b>                 |        |      | <b>21</b>  |
| <b>TOTAL First year ECTS ( at least 51 to leave)</b>   |                                   |        |      | <b>60</b>  |

**I ANNO STUDENTE UNIPIS (60 crediti)**

# Second year in Paris (Master Thesis in plasma physics)

| I SEMESTER (mandatory) 24 ECTS. Exams in december (if problems at max before May) |  |            |    |           |
|---|--|------------|----|-----------|
|   |  |            |    |           |
| 2014  | Introduction à la physique des Plasmas   | UE1        | 3  |           |
| 2015 and following year   | Outils pour les Plasmas et la Fusion   | TC1        | 3  |           |
| 2014  | Théorie cinétique  | UE2        | 3  |           |
| 2015 and following year   | Théorie Cinétique  | TC3        | 3  |           |
| 2014  | Modélisations fluides des plasmas  | UE3        | 3  |           |
| 2015 and following year   | Modélisation et simulation   | TC5        | 3  |           |
| 2014  | Magnétohydrodynamique  | UE4        | 3  |           |
| 2015 and following year   | Magnétohydrodynamique  | TC2        | 3  |           |
| 2014  | Plasmas spatiaux   | UE5        | 3  |           |
| 2015 and following year   | Ondes et Instabilités  | TC4        | 3  |           |
| 2014  | Concepts fondamentaux en physique des plasmas froids                                   | UE6        | 3  |           |
| 2015 and following year   | Physique atomique, moléculaire et rayonnement  | TC7        | 3  |           |
| 2014  | Instrumentation, diagnostics et analyse des plasmas                                    | UE7        | 6  |           |
| 2015 and following year   | Instrumentation, diagnostics et analyse des plasmas                                    | TC6        | 6  |           |
|   |  |            |    |           |
|   | UE7 ou TC6 : 6 ECTS will be counted as Stage/Thesis preparation in the second semester |            | -6 |           |
|   |  |            |    |           |
|   | <b>Totale ECTS</b>   |            | 18 |           |
|   |  |            |    |           |
| II SEMESTER - Stage/Thesis from January first to end of August                    |  |            |    |           |
|   |  |            |    |           |
|   | Stage (Master Thesis)  | 1 January  | 36 | 36        |
|   |  | -31 August |    |           |
|   | 6 ECTS counted as Stage/Thesis preparation in the first semester                       |            | 6  | 6         |
|   |  |            |    |           |
|   | <b>Totale ECTS</b>   |            |    | <b>42</b> |
|   |  |            |    |           |
| <b>TOTAL Second year ECTS</b>   |  |            |    | <b>60</b> |

A Tutor from UNIPi will follow the student career at UPMC

**II ANNO STUDENTE UNIPi (60 crediti)**





***GRAZIE!***